



Goniometrische formules

Goniometrische formules om te herleiden en/of vergelijkingen op te lossen:

Symmetrieformules	Verbanden tussen sin en cos
$\sin(-\alpha) = -\sin(\alpha)$	$\sin\left(\frac{1}{2}\pi - \alpha\right) = \cos(\alpha)$
$\cos(-\alpha) = \cos(\alpha)$	$\cos\left(\frac{1}{2}\pi - \alpha\right) = \sin(\alpha)$
$\tan(-\alpha) = -\tan(\alpha)$	
$\sin(\pi - \alpha) = \sin(\alpha)$	$\sin^2(\alpha) + \cos^2(\alpha) = 1$
$\cos(\pi - \alpha) = -\cos(\alpha)$	
$\tan(\pi - \alpha) = -\tan(\alpha)$	

Somformules	Verdubbelingsformules
$\sin(\alpha + \beta) = \sin(\alpha) \cdot \cos(\beta) + \cos(\alpha) \cdot \sin(\beta)$	$\sin(2\alpha) = 2 \sin(\alpha) \cos(\alpha)$
$\sin(\alpha - \beta) = \sin(\alpha) \cdot \cos(\beta) - \cos(\alpha) \cdot \sin(\beta)$	$\cos(2\alpha) = \cos^2(\alpha) - \sin^2(\alpha)$
$\cos(\alpha + \beta) = \cos(\alpha) \cdot \cos(\beta) - \sin(\alpha) \cdot \sin(\beta)$	$\cos(2\alpha) = 2 \cos^2(\alpha) - 1$
$\cos(\alpha - \beta) = \cos(\alpha) \cdot \cos(\beta) + \sin(\alpha) \cdot \sin(\beta)$	$\cos(2\alpha) = 1 - 2 \sin^2(\alpha)$

Formule voor $a \sin(x)$ plus $b \cos(x)$

$$a \cdot \sin(x) + b \cdot \cos(x) = \sqrt{a^2 + b^2} \sin(x + \beta) \text{ waarin } \tan(\beta) = \frac{b}{a}$$

